Combinations Question Bank

- 1. From a class of 12 boys and 10 girls, 10 students are to be chosen for a competition, at least including 4 boys and 4 girls. The 2 girls who won the prizes last year should be included. In how many ways can the selection be made? Ans: 104874
- 2. An examination paper consists of 12 questions divided into parts A and B. Part A contains 7 questions and part B contains 5 questions. A candidate is required to attempt 8 questions selecting at least 3 from each part. In how many ways can the candidate select the questions? Ans: 420
- 3. A committee is to be formed from 9 ladies and 8 gentlemen. In how many ways can a committee of 5 be formed so as to command a lady majority? Ans: 3486
- 4. Everybody in a room shakes hands with everybody else. The total number of handshakes is 66. Find the total number of persons in the room. Ans: 12

5. Find n if i)
$$n_{Cn-2} = 28$$
 ii) 3. $n_{C6} = 2.n_{C4}$
6. If $n_{C_8} = n_{C_2}$, find the value of n and n_{C_3}
7. If $n_{C_8} = n_{C6}$, find the value of n and n_{C2}
8. Determine n if i) $2n_{C_5} : n_{C_5} = 12:1$ ii) $2n_{C_5} : n_{C_5} = 11:1$
9. Find r if i) $50_{C_{r+8}} = 50_{C_{3r+2}}$ ii) $18_{C_4} = 118_{C_{r+2}}$ iii) $n_{P_r} = 24.n_{C_r}$
10. Find n and r if $n_{P_2} = 272$ and $n_{C_r} = 136$
11. If $n+1_{C_r} : n_{C_r} : n-1_{C_r} = 11:6:3$, find n and r
12. If $n_{Cr-1} = 36$, $n_{Cr} = 84$ and $n_{Cr+1} = 126$, find n and r. [ans: n = 9; r = 3]
13. If $15_{C_r} : 15_{C_{r-1}} = 11:5$, find r
14. If $n+2_{C_8} : n-2_{P_4} = 57:16$, find the value of n.
15. In how many ways a team of 3 boys and 3 girls be selected from 5 boys and 5
16. What is the number of ways of choosing 4 cards from a pack of 52 cards?
In how many of these
i) four cards of the same suit
ii) four cards belong to different suits
iii) are face cards
iv) two are red cards and two are black cards
v) cards of the same colour.

17. A polygon has 54 diagonals.

- i) Find the number of sides of the polygon
- ii) Find the total number of distinct triangles that can be formed using its vertices.

[Ans:220]

18. (i) There are 27 points in a plane. 5, 10 and 15 points are collinear on distinct lines. By joining these points, how many distinct lines can be formed ? [ans: 194]

5. Find n if i)
$$n_{Cn-2} = 28$$
 ii) 3. $n_{C6} = 2.n_{C4}$

- girls?

(ii) How many distinct triangles can be formed whose vertices are the given 27 points. [ans: 2340]

- 19. A test consists of 10 multiple choice questions each having four alternative answers of which exactly two are correct. A student has to mark two answers and his answer is considered correct only if both the selected answers are correct. Find the number of ways of getting exactly 8 correct answers by a student answering all the questions. [ans: 1125]
- 20. A student is to answer 10 out of 13 questions in an examination such that he must choose at least 4 from the first five questions. Find the number of choices available to him [ans: 196]