

The Indian School, Kingdom of Bahrain

Class : XI

Mathematics Assignment

Date of Submission: 02. 05. 2011

1. If $\tan x = k \tan y$; prove that $\sin(x - y) = \frac{k-1}{k+1} \sin(x+y)$

2. Show that $\cos 20^\circ \cos 40^\circ \cos 60^\circ \cos 80^\circ = \frac{1}{16}$

3. Prove that $\tan 8x - \tan 7x - \tan x = \tan 8x \tan 7x \tan x$

4. Prove that $\cos^2 x + \cos^2(x + 120^\circ) + \cos^2(x - 120^\circ) = \frac{3}{2}$

5. Prove that $\sqrt{2 + \sqrt{2 + 2 \cos 4x}} = 2 \cos x$

6. Prove that $\frac{\sin x \sin 2x + \sin 3x \sin 6x}{\sin x \cos 2x + \sin 3x \cos 6x} = \tan 5x$

7. Evaluate:
$$\frac{\cos(2\pi + \theta) \cos ec(2\pi + \theta) \tan(\frac{\pi}{2} + \theta)}{\sec(\frac{\pi}{2} + \theta) \cos(2\pi - \theta) \cot(\pi + \theta)}$$

8. Find the value of $\sin \frac{x}{2}$, $\cos \frac{x}{2}$ and $\tan \frac{x}{2}$ if $\tan x = \frac{-3}{4}$, x is in quadrant IV

9. Prove that $\frac{\cos 11^\circ + \sin 11^\circ}{\cos 11^\circ - \sin 11^\circ} = \tan 56^\circ$

10. Verify that $\frac{\sin x + \sin 3x + \sin 5x}{\cos x + \cos 3x + \cos 5x} = \tan 3x$

11. Prove that $\frac{\sin 5x + \sin 7x + \sin 9x + \sin 11x}{\cos 5x + \cos 7x + \cos 9x + \cos 11x} = \tan 8x$

12. If $\sin x = \frac{3}{5}$ and $\cos y = \frac{-12}{13}$, $0 < x < \pi/2$ and $\pi/2 < y < \pi$, then find $\sin(x - y)$.

13. If $\tan(\alpha + \theta) = n \tan(\alpha - \theta)$, Show that $(n+1)\sin 2\theta = (n-1)\sin 2\alpha$

14. Find the value of $\tan \frac{\pi}{8}$

15. Solve the following trigonometric equations:

i) $2 \cos^2 x + 3 \sin x = 0$ ii) $\sin x + \sin 2x + \sin 3x = 0$